# TALK TO CLIENTS ABOUT THE MERITS OF VARIABLE-RATE HOME LOANS. 

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## What's the most effective way for your clients to finance their mortgages?

Back in 2001, that very question prompted us to conduct an analysis that confirmed and documented that savings accrue to people who are willing to accept risk and finance a mortgage with a floating- or variable-rate loan. The IFID Centre's original research from that year proved our hypothesis and now, with the addition of six more years of data, we're able to reaffirm that over the long run, homeowners (your clients) really do pay extra for fixed-rate mortgages.

And, while the so-called premium for predictability has declined somewhat during the past five years as the yield curve has flattened, it remains an implicit opportunity cost for homebuyers who are averse to risk.

We also found short-term prophecy doesn't pay in the mortgage market. Even Canadians who can accurately predict the next move of the Bank of Canada, and lock in a mortgage just as the short rate is about to increase, are worse off on average compared with those who float over the entire interest-rate cycle. This is because properly timing the mortgage market requires an ability to predict movements of both short- and long-term points on the yield curve, a skill even Bank of Canada governor Mark Carney is unlikely to possess.

Back in 2001, we used some basic financial and statistical concepts to examine the relative benefits of financing a mortgage at a variable interest rate. At the time, we introduced the concept of the Maturity Value of Sav-
ings (MVS) from floating-a quantity which was computed by investing the difference between variable and fixed mortgage payments at the given 91-day Treasury-bill rate, and then accumulating this account over the amortization period. We found the value of this hypothetical account was positive the majority of the time, so the homeowner saved by using a variable-rate mortgage.

More specifically, the study showed that a positive MVS was generated on a theoretical home loan $88.6 \%$ of the time between 1950 and 2000. So a borrower was better off nearly $90 \%$ of the time by choosing a variable-rate mortgage over a fixed-rate mortgage. Of course, the converse (that the buyer is worse off $11.4 \%$ of the time) is also true. But the good really appears to outweigh the bad in this equation. The main reason for this result lies in the term structure of interest rates (the yield curve) which plots continued on page 27
continued from page 25 them on financial assets with varying maturities. Shortterm rates and long-term yields are not only different, but also can move in different directions on any given day (See "Floating Versus Fixed," this page).

The yield curve tends to slope upward, because assets with a longer time to maturity usually carry higher interest rates to compensate for the risk associated with rate changes during the term of the investment.

Over the past few years, a number of important developments have taken place in the mortgage market. Residential real estate prices have increased significantly across Canada, with average housing prices (as forecast by Royal LePage Real Estate Services) expected to pass the $\$ 300,000$ mark for the first time during 2008. In addition to the robust housing market, the Bank of Canada increased its interest rates in the summer of 2007, but then paused in its September rate setting. More recently, the Canadian dollar has hovered around a 30-year high relative to the U.S. dollar and the recent volatility in global equity markets has only increased the cloud of uncertainty around financial decision making.

All of this has prompted many people to wonder whether it's the right time to lock-in a fixed rate, long-term mortgage. This is a risk-versus-return decision that depends on a client's personal tolerance for fluctuating mortgage payments and interest rates. There's no one-size-fits-all solution.

## Updating the results

So, should you still go with the float? As in the original study, our examples assume two people are about to renew their mortgages and that each has three five-year terms remaining. Both have $\$ 100,000$ outstanding and are amortizing the balance over the next 15 years. One decides to go with a variable rate (floating) mortgage, while the other decides to lock-in at the fiveyear fixed rate (see, "Amortization Savings," page 29).

An example helps illustrate how to read the table. Assume a borrower took out a variable-rate mortgage in January 1964 and amortized the loan over 15 years. In the process of making regular monthly payments, this borrower invested the difference between what she would have paid if she'd had taken out

## Floating Versus Fixed

Changes in the spread between short-term (variable, prime) and long-term (five-year fixed) rates from January 2002 through December 2007.


Source: Five-year fixed rates obtained from the CANSIM II statistical database. Floating Rates obtained from Bank of Canada.
a traditional five-year, fixed-rate mortgage and what she would actually pay in 91-day Treasury bills each month. By January 1979, when the mortgage has matured, the borrower would have accumulated $\$ 20,970$. This number represents the MVS.

By early 2008, the frequency of having a positive MVS was up to $90.1 \%$ from $88.6 \%$ in 2001 , with the first 15 -year mortgage beginning in January, 1950. That is, you were better off $90.1 \%$ of the time if you had gone with a floating rate mortgage instead of the traditional five-year fixed-rate mortgage. The average magnitude of the MVS dropped slightly to $\$ 20,630$ from $\$ 22,210$ in the 2001 study. Of course, the numbers are across different periods of time.

Although we have been focusing on 15-year mortgages, let's suppose both homeowners only had 10 years remaining on their mortgages. Does it still pay to go with the float? (see "Mature Savings," page 33)

As you might expect, with a shorter amortization the average magnitude of the MVS declined to $\$ 11,334$. This is a result of having less time to grow the accumulated savings at the T-bill rate. However, the number of times a borrower comes out on top by choosing the variable rate is still quite high: $88 \%$. So it seems our earlier results are not sensitive to the amortization period.

An alternative way of illustrating the continued on page 29

# Amortization Savings 

The MVS: 15-year periods ended Jan 1965 through December 2007.
Mortgage Maturity Date

|  | JAN | FEB | MAR | APR | MAY | JUN | JUL | AUG | SEP | OCT | NOV | DEC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1965 | \$8,723 | \$8,648 | \$8,571 | \$8,492 | \$7,354 | \$7,274 | \$7,065 | \$6,785 | \$7,036 | \$7,222 | \$7,337 | \$7,251 |
| 1966 | \$7,166 | \$7,080 | \$7,193 | \$8,822 | \$10,461 | \$10,583 | \$11,740 | \$12,476 | \$13,508 | \$14,043 | \$14,375 | \$14,291 |
| 1967 | \$14,056 | \$14,170 | \$14,074 | \$13,838 | \$14,313 | \$14,828 | \$15,150 | \$15,255 | \$14,848 | \$15,106 | \$15,005 | \$14,698 |
| 1968 | \$15,330 | \$15,028 | \$14,518 | \$14,135 | \$14,000 | \$14,272 | \$14,168 | \$14,179 | \$14,801 | \$14,896 | \$15,147 | \$15,023 |
| 1969 | \$14,744 | \$14,622 | \$14,498 | \$13,707 | \$13,482 | \$13,567 | \$13,435 | \$13,910 | \$14,879 | \$14,746 | \$14,828 | \$14,686 |
| 1970 | \$14,621 | \$14,399 | \$14,199 | \$14,030 | \$11,664 | \$11,474 | \$11,095 | \$10,649 | \$11,037 | \$11,308 | \$11,542 | \$11,469 |
| 1971 | \$11,207 | \$11,073 | \$11,246 | \$11,022 | \$10,890 | \$11,200 | \$11,981 | \$13,582 | \$13,906 | \$15,022 | \$15,784 | \$15,738 |
| 1972 | \$16,008 | \$16,250 | \$16,063 | \$15,462 | \$14,863 | \$16,407 | \$16,730 | \$17,070 | \$ 17,881 | \$18,369 | \$18,346 | \$17,878 |
| 1973 | \$18,211 | \$17,719 | \$16,939 | \$16,461 | \$16,232 | \$16,030 | \$15,843 | \$16,097 | \$15,842 | \$16,092 | \$16,074 | \$15,953 |
| 1974 | \$16,718 | \$16,573 | \$16,464 | \$15,769 | \$15,300 | \$15,991 | \$16,241 | \$17,723 | \$19,951 | \$20,048 | \$20,541 | \$20,757 |
| 1975 | \$20,731 | \$20,326 | \$20,130 | \$20,047 | \$19,528 | \$19,342 | \$19,062 | \$19,514 | \$19,008 | \$18,501 | \$18,474 | \$18,716 |
| 1976 | \$18,167 | \$18,054 | \$17,311 | \$17,158 | \$17,246 | \$17,539 | \$18,078 | \$18,590 | \$18,624 | \$18,570 | \$18,109 | \$17,838 |
| 1977 | \$17,408 | \$16,792 | \$16,298 | \$15,053 | \$13,908 | \$15,909 | \$16,872 | \$16,838 | \$16,856 | \$18,615 | \$18,497 | \$18,127 |
| 1978 | \$19,270 | \$18,958 | \$19,406 | \$19,952 | \$19,811 | \$19,650 | \$19,488 | \$20,323 | \$19,945 | \$19,578 | \$19,663 | \$19,361 |
| 1979 | \$20,970 | \$20,692 | \$20,633 | \$21,160 | \$20,766 | \$21,916 | \$23,162 | \$25,030 | \$25,749 | \$26,012 | \$26,164 | \$26,816 |
| 1980 | \$25,792 | \$23,210 | \$22,258 | \$22,082 | \$22,293 | \$22,007 | \$22,979 | \$24,158 | \$24,431 | \$25,402 | \$24,651 | \$24,582 |
| 1981 | \$22,578 | \$21,577 | \$18,744 | \$18,269 | \$18,407 | \$19,119 | \$20,603 | \$21,994 | \$22,024 | \$21,588 | \$19,522 | \$17,774 |
| 1982 | \$15,478 | \$12,608 | \$11,404 | \$10,690 | \$10,607 | \$12,558 | \$13,899 | \$13,279 | \$12,791 | \$16,849 | \$16,001 | \$14,498 |
| 1983 | \$16,912 | \$15,722 | \$17,059 | \$20,374 | \$21,196 | \$21,268 | \$21,443 | \$21,904 | \$ 22,235 | \$21,649 | \$22,190 | \$21,599 |
| 1984 | \$25,163 | \$24,263 | \$23,856 | \$28,556 | \$31,257 | \$34,957 | \$39,357 | \$43,492 | \$47,400 | \$51,128 | \$53,725 | \$53,601 |
| 1985 | \$53,210 | \$46,012 | \$46,317 | \$50,935 | \$46,741 | \$45,281 | \$43,832 | \$45,526 | \$49,669 | \$51,242 | \$48,340 | \$46,237 |
| 1986 | \$40,766 | \$36,292 | \$30,241 | \$30,184 | \$32,114 | \$33,222 | \$33,958 | \$38,344 | \$37,099 | \$32,649 | \$22,903 | \$14,692 |
| 1987 | \$9,095 | \$3,529 | \$3,429 | \$2,539 | \$3,620 | \$5,037 | \$4,651 | \$1,551 | \$ $(2,956)$ | \$(7,686) | \$ $(12,405)$ | \$ $(16,227)$ |
| 1988 | \$ 20,540 ) | \$(24,230) | \$(25,334) | \$ $(25,573)$ | \$ 24,989 ) | \$ 24,160 ) | \$(22,327) | \$(19,563) | \$ 14,072 ) | \$(14,484) | \$(14,305) | \$(14,650) |
| 1989 | \$(17,138) | \$ 18,280 ) | \$(18,977) | \$(8,402) | \$1,666 | \$4,501 | \$9,160 | \$16,637 | \$22,329 | \$31,110 | \$36,523 | \$26,733 |
| 1990 | \$22,405 | \$9,824 | \$14,570 | \$29,306 | \$10,969 | \$5,113 | \$7,061 | \$11,499 | \$25,621 | \$31,443 | \$28,112 | \$30,152 |
| 1991 | \$25,346 | \$25,118 | \$28,968 | \$34,620 | \$42,412 | \$46,718 | \$47,788 | \$64,569 | \$63,967 | \$53,710 | \$39,129 | \$25,479 |
| 1992 | \$17,864 | \$12,938 | \$14,281 | \$12,436 | \$13,476 | \$12,043 | \$12,237 | \$6,439 | \$(3,527) | \$(14,576) | \$ $(25,597)$ | \$(30,229) |
| 1993 | \$ $(33,516)$ | \$(38,676) | \$(41,582) | \$(42,741) | \$(43,808) | \$(47,492) | \$(47,961) | \$(44,649) | \$ $(37,424)$ | \$(40,085) | \$ 37,400$)$ | \$(34,697) |
| 1994 | \$ $(38,407)$ | \$ 39,053$)$ | \$(38,779) | \$ 34,556 ) | \$(30,295) | \$ 27,786 ) | \$ $(24,586)$ | \$(19,326) | \$ 15,818 ) | \$562 | \$11,889 | \$ $(2,845)$ |
| 1995 | \$(8,362) | \$ 2,506 ) | \$21,779 | \$51,505 | \$9,863 | \$(8,075) | \$(6,394) | \$(2,184) | \$12,559 | \$17,942 | \$18,106 | \$24,692 |
| 1996 | \$20,457 | \$24,377 | \$30,531 | \$37,597 | \$53,891 | \$67,264 | \$75,349 | \$108,710 | \$113,980 | \$104,467 | \$82,958 | \$70,403 |
| 1997 | \$74,794 | \$82,916 | \$88,534 | \$89,939 | \$92,761 | \$94,508 | \$96,721 | \$92,473 | \$79,782 | \$65,726 | \$49,067 | \$44,947 |
| 1998 | \$42,964 | \$36,611 | \$32,014 | \$29,737 | \$30,135 | \$28,874 | \$29,852 | \$38,380 | \$43,423 | \$32,591 | \$28,593 | \$27,216 |
| 1999 | \$27,395 | \$27,006 | \$32,716 | \$45,111 | \$51,535 | \$53,516 | \$59,939 | \$53,924 | \$48,924 | \$46,366 | \$41,847 | \$38,553 |
| 2000 | \$36,565 | \$40,273 | \$51,764 | \$48,639 | \$46,382 | \$39,822 | \$38,014 | \$37,001 | \$37,224 | \$37,247 | \$34,122 | \$29,600 |
| 2001 | \$27,783 | \$27,744 | \$25,609 | \$20,273 | \$15,206 | \$18,275 | \$20,806 | \$20,374 | \$20,945 | \$19,136 | \$14,984 | \$12,736 |
| 2002 | \$9,438 | \$5,552 | \$4,884 | \$8,964 | \$13,973 | \$13,755 | \$11,272 | \$10,975 | \$12,414 | \$17,929 | \$14,076 | \$15,946 |
| 2003 | \$17,637 | \$15,395 | \$9,647 | \$9,059 | \$11,773 | \$13,044 | \$12,530 | \$17,345 | \$20,281 | \$16,661 | \$14,179 | \$16,853 |
| 2004 | \$16,789 | \$16,920 | \$22,833 | \$33,201 | \$31,109 | \$31,044 | \$35,633 | \$34,702 | \$33,872 | \$34,400 | \$35,781 | \$40,315 |
| 2005 | \$43,770 | \$47,729 | \$50,063 | \$56,033 | \$58,793 | \$56,758 | \$56,573 | \$56,159 | \$56,025 | \$54,603 | \$53,821 | \$49,169 |
| 2006 | \$44,906 | \$40,321 | \$41,214 | \$42,021 | \$42,570 | \$43,352 | \$44,421 | \$43,988 | \$42,982 | \$36,923 | \$29,458 | \$27,400 |
| 2007 | \$27,529 | \$27,382 | \$30,532 | \$35,710 | \$33,760 | \$29,692 | \$25,190 | \$20,897 | \$19,276 | \$23,551 | \$24,356 | \$26,849 |

NOTES: Result of investing the difference in monthly payments between fixed and variable at the $T$-bill rate of the appropriate period and continuing to do so for 15 years.

The MVS: 10-year periods ended Jan 1965 through December 2007.

Mortgage Maturity Date

|  | JAN | FEB | MAR | APR | MAY | JUN | JUL | AUG | SEP | OCT | NOV | DEC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1965 | \$7,309 | \$7,200 | \$7,089 | \$6,976 | \$5,439 | \$5,324 | \$5,035 | \$4,650 | \$4,978 | \$5,219 | \$5,364 | \$5,240 |
| 1966 | \$5,116 | \$4,990 | \$5,131 | \$5,003 | \$4,933 | \$5,133 | \$5,602 | \$6,616 | \$6,846 | \$7,622 | \$8,158 | \$8,147 |
| 1967 | \$8,408 | \$8,668 | \$8,652 | \$8,455 | \$8,257 | \$9,054 | \$9,124 | \$9,381 | \$9,946 | \$9,961 | \$9,978 | \$9,720 |
| 1968 | \$9,712 | \$9,427 | \$8,833 | \$8,407 | \$8,311 | \$8,266 | \$8,216 | \$8,324 | \$8,262 | \$8,483 | \$8,419 | \$8,354 |
| 1969 | \$8,575 | \$8,511 | \$8,445 | \$8,033 | \$7,901 | \$8,181 | \$8,175 | \$8,968 | \$10,415 | \$10,412 | \$10,698 | \$10,690 |
| 1970 | \$10,787 | \$10,681 | \$10,607 | \$10,582 | \$10,274 | \$10,237 | \$9,955 | \$10,113 | \$9,800 | \$9,333 | \$9,346 | \$9,484 |
| 1971 | \$9,376 | \$9,437 | \$9,380 | \$9,333 | \$9,303 | \$9,329 | \$9,415 | \$9,520 | \$9,475 | \$9,413 | \$9,363 | \$9,311 |
| 1972 | \$9,146 | \$8,946 | \$8,708 | \$7,932 | \$7,157 | \$8,122 | \$8,547 | \$8,538 | \$8,567 | \$9,218 | \$9,209 | \$9,112 |
| 1973 | \$9,582 | \$9,504 | \$9,627 | \$9,616 | \$9,401 | \$9,219 | \$9,056 | \$9,465 | \$9,210 | \$9,082 | \$9,134 | \$9,052 |
| 1974 | \$9,593 | \$9,484 | \$9,425 | \$9,082 | \$8,435 | \$8,749 | \$9,023 | \$9,805 | \$9,906 | \$9,963 | \$9,991 | \$10,216 |
| 1975 | \$9,583 | \$9,020 | \$8,728 | \$8,581 | \$8,419 | \$8,133 | \$8,838 | \$9,371 | \$9,224 | \$9,637 | \$9,549 | \$9,804 |
| 1976 | \$9,072 | \$8,903 | \$7,919 | \$7,696 | \$7,785 | \$8,141 | \$8,875 | \$9,575 | \$9,656 | \$9,627 | \$9,072 | \$8,770 |
| 1977 | \$8,270 | \$7,531 | \$6,955 | \$6,609 | \$ 6,361 | \$7,186 | \$7,864 | \$7,733 | \$7,668 | \$9,855 | \$9,650 | \$9,180 |
| 1978 | \$10,749 | \$10,437 | \$11,186 | \$12,808 | \$13,169 | \$13,171 | \$13,176 | \$13,299 | \$12,983 | \$12,643 | \$12,884 | \$12,622 |
| 1979 | \$14,835 | \$14,648 | \$14,748 | \$16,342 | \$17,022 | \$18,793 | \$20,777 | \$22,040 | \$23,422 | \$24,223 | \$24,875 | \$26,186 |
| 1980 | \$26,724 | \$24,572 | \$24,272 | \$24,569 | \$25,238 | \$25,426 | \$24,542 | \$24,978 | \$25,529 | \$25,833 | \$24,778 | \$23,493 |
| 1981 | \$21,517 | \$19,432 | \$15,876 | \$15,115 | \$14,986 | \$15,128 | \$15,481 | \$15,517 | \$15,021 | \$14,093 | \$10,889 | \$8,065 |
| 1982 | \$5,502 | \$2,530 | \$2,011 | \$1,641 | \$2,173 | \$3,006 | \$2,526 | \$1,367 | \$57 | \$(1,208) | \$(2,726) | \$(4,558) |
| 1983 | \$(6,858) | \$(8,637) | \$ $(9,282)$ | \$ $(9,505)$ | \$ $(9,194)$ | \$(8,442) | \$ $(7,558)$ | \$(6,565) | \$ $(4,409)$ | \$(4,338) | \$(4,587) | \$ $(5,035)$ |
| 1984 | \$ $(6,118)$ | \$(6,763) | \$ $(7,312)$ | \$ $(1,892)$ | \$3,041 | \$4,152 | \$6,241 | \$10,031 | \$13,000 | \$16,093 | \$17,986 | \$14,438 |
| 1985 | \$12,782 | \$4,897 | \$4,435 | \$9,530 | \$ 4,607 | \$3,594 | \$4,462 | \$6,235 | \$12,142 | \$14,524 | \$12,560 | \$12,713 |
| 1986 | \$10,617 | \$9,926 | \$11,510 | \$14,033 | \$16,568 | \$17,314 | \$17,016 | \$22,242 | \$21,455 | \$17,095 | \$11,914 | \$6,083 |
| 1987 | \$1,458 | \$(2,143) | \$ $(1,910)$ | \$(3,041) | \$(3,054) | \$(4,190) | \$(4,392) | \$(7,189) | \$(11,144) | \$ 115,364 ) | \$ $(19,166)$ | \$ 21,265 ) |
| 1988 | \$(23,003) | \$ $(25,108)$ | \$(26,271) | \$ 26,797$)$ | \$(27,727) | \$ 29,903$)$ | \$(30,578) | \$(30,295) | \$(27,149) | \$(27,264) | \$ 25,502$)$ | \$(24,062) |
| 1989 | \$(26,633) | \$(27,226) | \$(28,039) | \$ 27,264 ) | \$(25,730) | \$ 24,506 ) | \$ 23,433$)$ | \$(19,493) | \$(16,771) | \$(6,325) | \$1,491 | \$(7,264) |
| 1990 | \$(10,447) | \$ 7,592$)$ | \$5,626 | \$25,010 | \$ $(1,877)$ | \$ $(12,503)$ | \$ $(11,328)$ | \$(8,388) | \$1,093 | \$4,477 | \$5,006 | \$10,198 |
| 1991 | \$7,618 | \$10,377 | \$15,171 | \$21,176 | \$33,406 | \$42,175 | \$47,396 | \$70,904 | \$74,747 | \$68,550 | \$54,310 | \$46,007 |
| 1992 | \$49,956 | \$56,587 | \$60,700 | \$61,012 | \$62,160 | \$63,592 | \$65,846 | \$63,006 | \$53,548 | \$42,081 | \$30,755 | \$27,451 |
| 1993 | \$25,639 | \$21,409 | \$19,235 | \$17,605 | \$17,316 | \$16,065 | \$16,838 | \$22,045 | \$25,123 | \$17,825 | \$15,672 | \$14,107 |
| 1994 | \$14,360 | \$14,107 | \$16,927 | \$23,282 | \$28,460 | \$30,037 | \$33,636 | \$29,850 | \$26,585 | \$24,880 | \$21,539 | \$18,275 |
| 1995 | \$16,249 | \$18,295 | \$26,347 | \$23,128 | \$21,379 | \$17,228 | \$16,070 | \$15,395 | \$15,678 | \$16,129 | \$14,122 | \$11,850 |
| 1996 | \$11,512 | \$12,532 | \$10,677 | \$6,634 | \$2,953 | \$5,029 | \$6,639 | \$6,513 | \$7,039 | \$6,992 | \$5,533 | \$4,338 |
| 1997 | \$1,807 | \$ $(1,064)$ | \$(2,171) | \$(357) | \$3,655 | \$4,317 | \$3,377 | \$3,864 | \$5,149 | \$8,313 | \$5,286 | \$6,109 |
| 1998 | \$7,290 | \$5,672 | \$2,071 | \$1,727 | \$3,524 | \$4,441 | \$4,268 | \$7,736 | \$9,622 | \$7,574 | \$6,523 | \$8,961 |
| 1999 | \$9,424 | \$9,613 | \$12,740 | \$18,567 | \$16,599 | \$15,651 | \$17,676 | \$17,117 | \$17,166 | \$17,587 | \$18,380 | \$21,237 |
| 2000 | \$23,113 | \$26,275 | \$29,239 | \$34,377 | \$37,401 | \$36,610 | \$36,962 | \$36,199 | \$36,158 | \$35,436 | \$35,078 | \$32,056 |
| 2001 | \$29,694 | \$26,522 | \$27,016 | \$27,105 | \$27,337 | \$27,786 | \$28,586 | \$29,005 | \$28,679 | \$24,838 | \$19,882 | \$18,149 |
| 2002 | \$17,888 | \$17,744 | \$19,967 | \$22,947 | \$21,504 | \$18,660 | \$15,548 | \$12,452 | \$11,325 | \$14,861 | \$15,520 | \$17,194 |
| 2003 | \$17,228 | \$16,974 | \$14,265 | \$13,659 | \$13,787 | \$13,584 | \$12,504 | \$12,175 | \$12,469 | \$11,206 | \$7,493 | \$6,216 |
| 2004 | \$4,045 | \$3,345 | \$7,508 | \$15,577 | \$16,407 | \$18,918 | \$24,307 | \$23,094 | \$21,146 | \$20,696 | \$21,269 | \$23,626 |
| 2005 | \$26,219 | \$26,080 | \$23,037 | \$21,957 | \$19,111 | \$17,508 | \$16,856 | \$19,182 | \$19,508 | \$18,681 | \$18,398 | \$17,152 |
| 2006 | \$14,580 | \$13,435 | \$15,047 | \$16,996 | \$17,355 | \$17,703 | \$17,821 | \$15,243 | \$14,272 | \$11,433 | \$8,358 | \$8,128 |
| 2007 | \$9,081 | \$8,839 | \$8,797 | \$11,751 | \$11,124 | \$9,708 | \$8,191 | \$7,703 | \$7,186 | \$5,877 | \$5,574 | \$6,549 |

continued from page 31 benefits of going with the float is to look at the Total Months Saved (TMS). TMS is computed by making the monthly payment on the variable rate mortgage identical to the five-year fixed-monthly payment. Using this approach you can determine how much sooner the mortgage would have been paid off by going with a vari-able-rate mortgage (see "Total Months Saved," page 35).

Updated results show the TMS was positive $79.2 \%$ of the time (up from $74 \%$ in the 2001 study) for 15-year mortgages maturing from January 1984 to December 1999, with an average savings of 19.3 months (up from 18 months in the original study which covered a period between January 1984 and December 1999). In other words, floating lets people typically shave more than a year off the time it took to get free and clear of a home loan. By including mortgages maturing from January 1965 to December 1983, the TMS becomes positive $88.4 \%$ of the time, with an average savings of 19.2 months. If the amortization is reduced to 10 years, the mortgage would have been paid off sooner $90.5 \%$ of the time, with an average savings of 8.6 months.

The results were also replicated to take into account the impact negotiating mortgage rates can have on the MVS and the TMS. The negotiator is assumed to have the ability to bargain a 100-basis point reduction on the five-year fixed rate, and a 50-basis point reduction in the variable rate (see "Reaping Rewards," page 33). From a methodological point of view, we assumed the variable rate was the commercial prime rate, which is the convention in practice.

The result is a positive MVS 84.9\% of the time and a positive TMS $84.5 \%$ of the time. The aggressive negotiator,

# Reaping Rewards 

Frequency in which a borrower obtained a positive MVS over the 15-year periods from January, 1965 through December 31, 2007 given the borrower's ability to negotiate.

|  | Maturity Value of Savings (MVS) January 1965 - December 2007 |  |  |
| :---: | :---: | :---: | :---: |
|  | NO NEGOTIATION | NEGOTIATOR | AGGRESSIVE |
| Reduction (fixed/float) | - | 100bp/50bp | 150bp/75bp |
| Positive | 90.12\% | 85.08\% | 77.13\% |
| Negative | 9.88\% | 14.92\% | 22.87\% |

Frequency of a positive MVS over the 10-year periods ending from January, 1965 through December 31, 2007 given the borrower's ability to negotiate.

|  | Maturity Value of Savings (MVS) January 1965 - December 2007 |  |  |
| :---: | :---: | :---: | :---: |
|  | NO NEGOTIATION | NEGOTIATOR | AGGRESSIVE |
| Reduction (fixed/float) | - | 100bp/50bp | 150bp/75bp |
| Positive | 87.98\% | 81.59\% | 75.97\% |
| Negative | 12.02\% | 18.41\% | 24.03\% |

Frequency in which the borrower paid off the mortgage sooner given his or her ability to negotiate over the 15-year periods ending from January, 1965 through December 31, 2007.

|  | Total Months Saved (TMS) January 1965 - December 2007 |  |  |
| :---: | :---: | :---: | :---: |
|  | NO NEGOTIATION | NEGOTIATOR | AGGRESSIVE |
| Reduction (fixed/float) | - | 100bp/50bp | 150bp/75bp |
| Positive | 88.37\% | 84.88\% | 77.91\% |
| Negative | 11.63\% | 15.12\% | 22.09\% |

Frequency in which the borrower paid off the mortgage sooner given his or her ability to negotiate over the 10-year periods ending from January, 1965 through December 31, 2007.

|  | Total Months Saved (TMS) January 1965 - December 2007 |  |  |
| :---: | :---: | :---: | :---: |
|  | NO NEGOTIATION | NEGOTIATOR | AGGRESSIVE |
| Reduction (fixed/float) | - | 100bp/50bp | 150bp/75bp |
| Positive | 90.50\% | 81.01\% | 72.48\% |
| Negative | 9.50\% | 18.99\% | 27.52\% |

NOTE: All four tables assume a negotiator is able to obtain a 100-basis point reduction on the five-year fixed rate and a 50 basis point reduction on the floating rate of interest. It also assumes an aggressive negotiator is able to obtain a 150 -basis point reduction on the five-year fixed rate and a 75 -basis point reduction on the floating rate of interest.

## Total Months Saved

Data represents the TMS by borrowing at prime versus the five-year rate. The year and month correspond to the maturity of the 15-year amortization period.

Mortgage Maturity Date

|  | JAN | FEB | MAR | APR | MAY | JUN | JUL | AUG | SEP | OCT | NOV | DEC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1965 | 11.7 | 11.6 | 11.5 | 11.4 | 10.0 | 9.9 | 9.6 | 9.2 | 9.6 | 9.8 | 9.9 | 9.8 |
| 1966 | 9.7 | 9.6 | 9.7 | 11.9 | 14.1 | 14.5 | 15.9 | 16.7 | 18.0 | 18.6 | 18.9 | 18.8 |
| 1967 | 18.5 | 18.6 | 18.5 | 18.2 | 18.9 | 19.4 | 19.4 | 19.5 | 18.9 | 19.2 | 19.2 | 18.8 |
| 1968 | 19.6 | 19.2 | 18.6 | 18.2 | 18.0 | 18.3 | 18.1 | 18.0 | 18.8 | 18.9 | 19.1 | 19.0 |
| 1969 | 18.6 | 18.4 | 18.3 | 17.3 | 17.1 | 17.1 | 17.0 | 17.4 | 18.3 | 18.2 | 18.2 | 18.0 |
| 1970 | 17.9 | 17.7 | 17.5 | 17.3 | 14.5 | 14.3 | 13.9 | 13.3 | 13.8 | 14.2 | 14.5 | 14.2 |
| 1971 | 13.9 | 13.8 | 14.0 | 13.8 | 13.7 | 14.1 | 15.0 | 16.8 | 17.3 | 18.6 | 19.4 | 19.4 |
| 1972 | 19.8 | 20.2 | 20.1 | 19.7 | 19.2 | 20.8 | 21.2 | 21.6 | 22.5 | 22.7 | 22.8 | 22.0 |
| 1973 | 22.3 | 21.4 | 20.5 | 19.9 | 19.5 | 19.3 | 19.3 | 19.5 | 19.4 | 19.7 | 19.7 | 19.5 |
| 1974 | 20.0 | 19.9 | 19.4 | 18.6 | 18.1 | 18.3 | 18.0 | 19.5 | 21.8 | 21.8 | 22.2 | 22.3 |
| 1975 | 22.2 | 21.8 | 21.5 | 21.4 | 20.8 | 20.6 | 20.6 | 21.0 | 20.4 | 19.8 | 20.1 | 20.3 |
| 1976 | 20.3 | 20.2 | 20.1 | 20.0 | 20.0 | 20.3 | 20.8 | 21.2 | 21.2 | 21.4 | 21.3 | 21.2 |
| 1977 | 20.9 | 20.4 | 20.0 | 18.9 | 17.8 | 19.7 | 20.7 | 20.8 | 20.9 | 22.5 | 22.5 | 22.3 |
| 1978 | 23.4 | 23.3 | 23.7 | 23.9 | 23.5 | 22.9 | 22.7 | 23.1 | 22.2 | 21.9 | 22.0 | 21.4 |
| 1979 | 22.7 | 22.5 | 22.3 | 21.7 | 20.6 | 21.5 | 22.0 | 23.5 | 23.9 | 23.9 | 24.2 | 24.6 |
| 1980 | 23.9 | 22.6 | 22.2 | 21.9 | 21.9 | 21.5 | 22.4 | 23.4 | 22.9 | 23.7 | 23.2 | 23.2 |
| 1981 | 21.5 | 20.7 | 18.0 | 17.5 | 17.6 | 18.2 | 19.4 | 20.5 | 20.5 | 20.2 | 19.0 | 18.2 |
| 1982 | 16.7 | 15.1 | 14.2 | 13.7 | 13.7 | 15.8 | 17.1 | 16.8 | 16.6 | 20.1 | 19.7 | 18.8 |
| 1983 | 21.0 | 20.4 | 21.3 | 23.7 | 24.5 | 24.7 | 24.9 | 25.1 | 25.0 | 24.2 | 24.3 | 23.9 |
| 1984 | 26.7 | 26.2 | 26.1 | 29.4 | 31.0 | 33.6 | 36.4 | 38.5 | 40.5 | 41.6 | 42.5 | 43.3 |
| 1985 | 43.5 | 39.6 | 39.0 | 40.0 | 40.1 | 40.1 | 39.2 | 40.1 | 41.6 | 42.2 | 40.5 | 38.0 |
| 1986 | 34.6 | 31.3 | 26.3 | 25.3 | 25.1 | 25.1 | 24.8 | 25.4 | 24.9 | 22.4 | 16.8 | 9.4 |
| 1987 | 4.3 | -2.5 | -4.2 | -5.7 | -4.7 | -6.2 | -5.0 | -6.5 | -9.9 | -12.9 | -17.2 | -21.1 |
| 1988 | -25.6 | -29.2 | -31.0 | -29.3 | -28.6 | -27.4 | -24.9 | -21.1 | -14.3 | -15.0 | -14.9 | -15.4 |
| 1989 | -18.4 | -19.9 | -22.4 | -9.1 | 0.7 | 2.6 | 5.6 | 13.3 | 18.2 | 25.1 | 29.0 | 22.8 |
| 1990 | 19.8 | 8.1 | 10.9 | 22.7 | 9.9 | 5.4 | 7.2 | 11.2 | 21.9 | 26.1 | 23.7 | 24.9 |
| 1991 | 20.9 | 19.0 | 22.6 | 27.1 | 32.5 | 34.7 | 35.2 | 43.9 | 43.4 | 37.8 | 29.7 | 20.9 |
| 1992 | 15.6 | 11.6 | 13.2 | 11.3 | 11.7 | 10.6 | 10.7 | 5.6 | -2.7 | -12.2 | -23.8 | -29.1 |
| 1993 | -32.9 | -39.7 | -44.1 | -49.0 | -50.6 | -60.7 | -62.0 | -59.9 | -51.0 | -56.5 | -52.0 | -50.8 |
| 1994 | -58.7 | -65.7 | -74.2 | -64.2 | -56.0 | -51.9 | -46.3 | -36.9 | -31.2 | -7.4 | 6.2 | -12.2 |
| 1995 | -20.6 | -14.7 | 13.9 | 39.1 | -1.0 | -28.1 | -25.9 | -17.8 | 2.9 | 8.7 | 9.4 | 17.0 |
| 1996 | 13.2 | 18.0 | 24.1 | 31.1 | 44.8 | 54.1 | 59.4 | 79.1 | 82.2 | 77.9 | 66.3 | 58.6 |
| 1997 | 62.2 | 68.2 | 71.7 | 72.1 | 73.6 | 75.3 | 77.5 | 75.6 | 67.5 | 56.8 | 44.4 | 41.2 |
| 1998 | 39.6 | 34.6 | 31.5 | 29.6 | 29.8 | 28.6 | 29.7 | 36.7 | 40.7 | 31.9 | 29.1 | 27.8 |
| 1999 | 28.1 | 27.9 | 32.1 | 40.7 | 46.0 | 47.4 | 51.4 | 47.4 | 44.0 | 42.1 | 38.5 | 35.0 |
| 2000 | 32.6 | 35.5 | 45.1 | 42.2 | 40.7 | 35.5 | 34.1 | 33.1 | 33.3 | 33.5 | 30.9 | 27.2 |
| 2001 | 26.1 | 26.6 | 24.5 | 19.3 | 14.2 | 17.3 | 19.9 | 20.0 | 20.7 | 20.0 | 16.7 | 14.7 |
| 2002 | 11.2 | 7.2 | 6.3 | 10.4 | 15.8 | 15.9 | 13.7 | 13.6 | 15.3 | 20.5 | 16.2 | 17.6 |
| 2003 | 19.4 | 16.7 | 10.3 | 9.7 | 12.7 | 14.1 | 13.6 | 19.0 | 21.5 | 18.0 | 15.6 | 18.9 |
| 2004 | 19.0 | 19.2 | 25.2 | 35.3 | 33.1 | 32.6 | 36.5 | 35.5 | 35.2 | 35.6 | 36.8 | 40.8 |
| 2005 | 43.6 | 47.1 | 49.9 | 55.4 | 58.1 | 57.0 | 57.3 | 56.8 | 56.8 | 55.9 | 55.4 | 51.7 |
| 2006 | 48.4 | 44.2 | 45.2 | 45.7 | 46.1 | 46.7 | 47.7 | 47.8 | 47.3 | 42.0 | 34.9 | 32.7 |
| 2007 | 32.8 | 32.6 | 35.8 | 40.5 | 38.6 | 34.5 | 29.8 | 25.2 | 23.4 | 28.4 | 29.4 | 32.1 |

continued from page 35 on the other hand, is able to negotiate a 150 -basis point reduction on the five-year fixed rate and a 75 -basis point reduction on the variable rate. In this case, the result is a positive MVS $77.1 \%$ of the time, while the TMS remained positive $77.9 \%$ of the time. The figures presented are based on 15-year mortgage amortizations. As one would suspect, people who can negotiate better rates than those posted by the banks erode some of the advantage of going floating over fixed.

## Locking in

Could you be even better-off by timing the market?

Well, let's take a hypothetical look at two individuals who each have $\$ 100,000$ outstanding on their respective mortgages. The balance will be amortized over the next 15 years with three fiveyear terms. One person decides to go with a pure float (variable-rate mortgage), while the other chooses to try and time the market. In timing the market, it's assumed the individual is able to accurately forecast Bank of Canada interest rates over the next year-beginning on January 1 of each year-and based on this will decide whether to float or fix the mortgage payments. The person floats where prime rates are falling over the next year and goes fixed when they are rising. Where a fixed-rate mortgage is selected, the individual must lock-in for the remainder of the five-year term and the process is repeated at the beginning of the following term (see, "Timing Troubles," page).

Contrary to what you might expect, it turns out the homeowner who went with the pure float mortgage outperformed the five-year fixed mortgage more often ( $88.1 \%$ ) than the individual who chose the market timing strategy ( $83.3 \%$ ). The average magnitude of

## Timing Troubles

An individual takes out a 15-year mortgage in January, 1982 with three five-year terms. He decides to go with a variable-rate mortgage for the first two years and then lock-in a fixed rate for the remaining three because rates were rising. Chart shows interest rate performance (fixed and floating) over the five-year term.


Rate source: Bank of Canada.
the MVS was also higher with the pure float $(\$ 15,821)$ when compared to market timing $(\$ 14,495)$. In absolute terms, the magnitude of the gains was higher $69 \%$ of the time by going with the pure float strategy over market timing.

Here is one historical example that should help illustrate why predictability may not necessarily pay off (See "Go With the Float," page 39). An individual finances a mortgage at a variable rate starting in January 1982. It is amortized over 15 years, which implies three five-year terms. Now, given the ability to foresee the direction of shortterm Bank of Canada interest rates at the beginning of each year, this clairvoyant individual decides to stick with a variable-rate mortgage for the first two years until January 1984. Then, with three years remaining on his original five-year contract, he decides to lockin at the fixed rate in January 1984 be-
cause he knows with $100 \%$ certainty that interest rates were rising in that year. So, he locks in for the remaining three years (1984 through 1986) at the three-year rate. However, a brief in-terest-rate spike reversed itself later in the year. For a few months, the floating rate pierced through the fixed rate and the decision to lock-in paid off. But for most of the remaining months, the short rate fell under the fixed rate and the original savings were washed away.

In other words, nobody owns a crystal ball. Being able to predict the path of short-term interest rates does not necessarily generate better odds over time.

In the calm, early summer of 2007, before the sub-prime mortgage crisis hit international headlines and markets, many Canadian commentators were predicting that official Bank of Canada interest rates had nowhere to go but up. And, on continued on page 39
continued from page 37 July 10th 2007, the Bank of Canada did in fact raise its overnight rate, partially validating those prognostications. But two months later, the global environment had changed dramatically and by December 4th, 2007, the Bank of Canada had to reverse its decision.
Nobody can truly predict how rates will move over a five-year period. It's just that simple. In updating our data to 2008, we confirmed that savings accrue to homeowners who eschew the temptation to forecast interest rates and are willing to accept risk and finance a mortgage with a floating- or variable-rate loan.

The results we obtained in 2001 continue to hold. Over the long run homeowners incur a cost for mortgage stability. On the other hand, we acknowledge that the so-called premium for predictability has indeed declined during the past five years as the yield curve has flattened. Your clients are no longer paying as much for the security of a fixed-rate mortgage. But they are still paying.

Practically speaking, we interpret the updated data as further evidence mortgage financing continues to be a risk-and-reward decision that must be integrated within the client's personal balance sheet and risk-management strategy. The stability and composition of a client's job, the amount of equity in his or her home, the asset allocation of the client's RRSP and whether he or she has a pension, should all be weighed as part of the mortgage financing decision. We continue to urge individual Canadians to avoid the temptation to outguess the Bank of Canada or the billion-dollar bond market. You owe it to your clients to do the same. ${ }^{\text {AE }}$

MILEVSKY \& WALKER

## Go With the Float

MVS from mortgage timing the market.

| GAINS FROM MORTGAGE PERIOD | MARKET TIMING OVER FIXED | GAINS FROM FLOATING OVER FIXED | MARKET TIMER BETTER OFF COMPARED TO FLOATER |
| :---: | :---: | :---: | :---: |
| 1967-1982 | \$7,236 | \$15,478 | NO |
| 1968-1983 | \$0 | \$16,912 | NO |
| 1969-1984 | \$0 | \$25,163 | NO |
| 1970-1985 | \$47,746 | \$53,210 | NO |
| 1971-1986 | \$31,892 | \$40,766 | NO |
| 1972-1987 | \$26,739 | \$9,095 | YES |
| 1973-1988 | \$3,634 | \$ 20,540 ) | YES |
| 1974-1989 | \$0 | \$(17,138) | YES |
| 1975-1990 | \$13,042 | \$22,405 | NO |
| 1976-1991 | \$3,810 | \$25,346 | NO |
| 1977-1992 | \$51,481 | \$17,864 | YES |
| 1978-1993 | \$12,894 | \$(33,516) | YES |
| 1979-1994 | \$0 | \$ $(38,407)$ | YES |
| 1980-1995 | \$13,995 | \$(8,362) | YES |
| 1981-1996 | \$18,509 | \$20,457 | NO |
| 1982-1997 | \$68,713 | \$74,794 | NO |
| 1983-1998 | \$26,131 | \$42,964 | NO |
| 1984-1999 | \$0 | \$ 27,395 | NO |
| 1985-2000 | \$36,401 | \$20,988 | YES |
| 1986-2001 | \$ 32,982 | \$15,345 | YES |
| 1987-2002 | \$12,841 | \$4,316 | YES |
| 1988-2003 | \$11,909 | \$9,113 | YES |
| 1989-2004 | \$(1,369) | \$9,078 | NO |
| 1990-2005 | \$37,025 | \$24,111 | YES |
| 1991-2006 | \$40,982 | \$25,953 | YES |

## BETTER OFF MARKET TIMING

## YES <br> NO <br> 30.95\% <br> 69.05\%

PERCENTAGE (\%)

